

# Assignment 8

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1. Using the “ $X$ ” data in the spreadsheet “Assignment 8.xls”
  - a. Compute the 95% confidence interval for a small sample assuming that  $X$  is distributed normally with an unknown mean and variance.
  - b. Compute the 95% confidence interval for a large sample assuming that  $X$  is distributed normally with an unknown mean and variance (hint, use the concentrated normal likelihood function).
  - c. In each case, test the hypothesis that the mean is equal to 5.3.
2. Using the “ $Y$ ” data in the spreadsheet “Assignment 8.xls”
  - a. Compute the 95% confidence level using the central limit theorem and test the hypothesis that the mean is equal to 5.3.
  - b. Given that the distribution is a Gamma distribution, construct a maximum likelihood estimate of  $\alpha$  and  $\beta$ . Construct a 95% confidence interval for each parameter.
  - c. Test the hypothesis that the mean of the Gamma distribution is equal to 5.3 (i.e., impose the restriction that  $\alpha\beta = 5.3$  this will give you a restricted likelihood function).